

## Alg. 2 Warm Up # 5-2

- Find the slope of the line through the points:  
(-2, 0) and (0, 1).
- Find the slope of the line perpendicular to the line above.
- What is the relationship between slopes of perpendicular lines?
- Find an equation of the line perpendicular to  $y = 3x + 4$ , that passes through the points:  
a) (0, 6)    b) (-7, 13)    c) (0.4, -1.2)    d) (8, 1)

Homework Questions: White worksheet

$$\begin{aligned}
 3) & 6x^2y^4 \cdot 4x^{-6}y \\
 & 6 \cdot 4 \cdot x^2 \cdot x^{-6} \cdot y^4 \cdot y^1 \\
 & 24 \cdot x^{-4}y^5 \\
 & \frac{24y^5}{x^4}
 \end{aligned}$$

$$\begin{aligned}
 1) & (5x)^2(15x^5)^{-1} \\
 & \frac{25x^2}{1} \cdot \frac{1}{15x^5} \\
 & \frac{25x^2}{15x^5} \\
 & \frac{5}{3x^3}
 \end{aligned}$$

$$\begin{aligned}
 6) & g(f(10)) \\
 & g\left(\frac{6}{10-2}\right) \\
 & g\left(\frac{3}{4}\right) \\
 & \sqrt{\frac{3}{4} - \frac{3}{4}} \\
 & \sqrt{\frac{12}{4} - \frac{3}{4}} \\
 & \sqrt{\frac{9}{4}} \\
 & \boxed{\frac{3}{2}}
 \end{aligned}$$

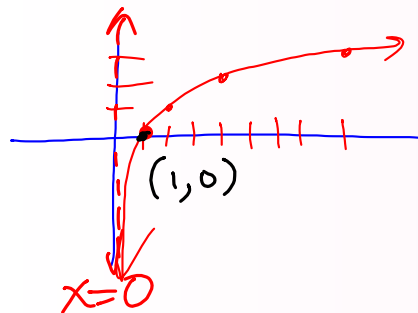
$$x^{2-5} = x^{-3}$$

7.  $y = \log_2 x$

Same as

$$2^y = x$$

x	y
1	0
2	1
4	2
8	3

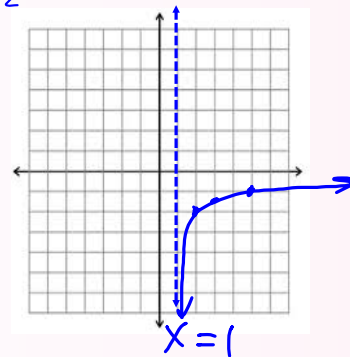


$$y = \frac{1}{2} \log_2(x-1) - 2$$

Rt 1, vertical compression  $\frac{1}{2}$ , down 2

x	y
2	0
3	$\frac{1}{2}$
5	1
9	$\frac{3}{2}$

x	y
2	-2
3	$-\frac{3}{2}$
5	-1
9	$-\frac{1}{2}$



8) 
$$\frac{3}{(x-4)(x+1)} + \frac{6}{(x+1)} \frac{(x-4)}{(x-4)}$$

$$\frac{3+6x-24}{(x-4)(x+1)}$$

$$\frac{6x-21}{(x-4)(x+1)}$$

$$\frac{3(2x-7)}{(x-4)(x+1)}$$

$$11) \frac{x+2}{x^2-9} - \frac{1}{x+3}$$

$$\frac{x+2}{(x+3)(x-3)} - \frac{1}{(x+3)(x-3)}$$

$$12) \frac{ab}{1} \left( \frac{1}{a} + \frac{1}{b} \right)$$

122

$$\frac{\cancel{ab}}{1} \cdot \frac{1}{\cancel{a}} + \frac{\cancel{ab}}{1} \cdot \frac{1}{\cancel{b}}$$

$$b + a$$

$$13) \frac{cd}{1} \left( \frac{3}{c} + \frac{2c}{d} \right)$$

$$\frac{\cancel{3}d}{\cancel{c}} + \frac{2\cancel{c}^2d}{\cancel{d}}$$

$$3d + 2c^2$$

$$15) \frac{18x^{-3}}{3xy^2} \cdot \frac{10(xy)^3}{12x^{-5}}$$

$$\frac{\cancel{6}}{x^4y^2} \cdot \frac{5\cancel{2}x^3y^3x^5}{\cancel{6}}$$

$$\frac{5x^8y^3}{x^4y^2}$$

$$\boxed{5x^4y}$$

CP's: 6 - #1 ----&gt; 6 (green) p. 257

## 6.1.1 How can I plot points in three dimensions?



## Creating a Three-Dimensional Model

In geometry, you worked with objects that existed in different dimensions. You considered lines and line segments, which have only one dimension: length. You also looked at flat shapes like circles, rectangles, and trapezoids that have two dimensions: length and width. Prisms, cones, and most objects that you encounter in the real world have volume, and therefore have three dimensions: length, width and height.

When you worked with graphs in Algebra 1, you represented points, the number line, and curves on a **two-dimensional** (flat) surface called the  $xy$ -plane. So far, you have only been able to represent relationships with at most two unknowns, usually the variables  $x$  and  $y$ . However, many problems, like some that you may have done in homework problems in Chapter 6, have more than two unknowns. Today, you and your team will build a model that will help you graph in three dimensions. As you work on this lesson, consider the following questions with your team:

How can we plot a point in three dimensions?

How can we write the coordinates of a point in three dimensions?


How can we show three dimensions on flat paper?

## together:

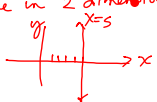
6-1. Consider when it is appropriate to graph a situation in one, two, and/or three dimensions. It may be helpful to think about your experience representing numbers and relationships on a number line or an  $xy$ -plane, and how you can adapt your knowledge to work in three dimensions. Discuss each question with your team before writing your response.

- How can you represent the solution to  $x = 5$  graphically? Can you think of more than one way?
- How can you represent the solutions to  $x + 2y = 5$  graphically?
- How could you represent the solutions to  $x + 2y + z = 5$ ? What would the solutions look like? Discuss these questions with your team and write down any ideas that you have.

a)  $x = 5$  is a point on the number line in one dimension:



or it is a vertical line in 2 dimensions, on the  $xy$ -plane.



## Resource Managers:

Scissors

Tape

Cup of cubes

One resource page for each person on your team



(rather than the outside). The result should look similar to the diagram at right.

6-3. Place a penny (or other marker) on the bottom surface of your model at the point where  $x = 4$  and  $y = 2$ . Now lift your marker straight up so that it you are holding it 3 units above the bottom of the model.

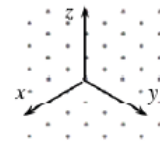
a. With your team, find a way to write the coordinates of this point.  $(4, 2, 3)$

b. In your model, find the point where  $x = 3$ ,  $y = 4$ , and  $z = 2$ . Use your team's method to write the coordinates for this point.

c. The model you have created is only a portion of the entire coordinate system used to represent three dimensions mathematically. How many of these models would you have to put together to create a model that represents the entire three-dimensional coordinate system? Think about the regions you would need to graph points like  $(5, -2, -7)$  or  $(-1, -2, -4)$ .

6-4. Use cubes to build each shape described below inside your three-dimensional model. Make sure that one corner of each shape you build lies at the **origin** (at the point  $(0, 0, 0)$ ).

- Build a  $2 \times 2 \times 2$  cube. Use coordinates to name the vertex that is farthest from the origin.
- Build a rectangular prism that is 2 units in length along the  $x$ -axis, 1 unit in length along the  $y$ -axis, and 3 units in length along the  $z$ -axis. Use coordinates to name the vertex that is farthest from the origin.
- Draw and label a three-dimensional coordinate system on isometric dot paper, as shown at right. Now add the prism from part (b) to the drawing. On your dot paper, label the coordinates of *all* of the vertices.



- 6-5. Build a rectangular prism that will have vertices in your model at  $(1, 0, 0)$ ,  $(0, 0, 4)$ , and  $(0, 3, 0)$ .
- Find the coordinates of the other five vertices.
  - Move the rectangular prism so that three vertices are at  $(-1, 0, 0)$ ,  $(0, 0, 4)$ , and  $(0, 3, 0)$ . Now where are the other vertices?
  - Is it possible to build another rectangular prism that has the same coordinates for the vertex farthest from the origin as the prism in part (b)? Be sure to justify your conclusion.

- 6-6. On isometric dot paper, draw a three-dimensional coordinate system and plot the following points:  $(0, 1, -1)$ ,  $(1, 2, 0)$ , and  $(2, 3, 1)$ .
- What do you notice about the three points?
  - With your team, find a strategy to make each point clearly different from the others. Be prepared to share your strategy with the class.
  - Identify the coordinates of two points that appear to be the same as  $(-2, 0, 0)$ .

HW: 6 -

# 8 ---> 13